

The advantage looked for is that, whilst all desirable accuracy is obtained, it can be worked with logarithms restricted to four places, and thereby lightens the labour of calculation, and to some degree also the chance of errors in computation.

Let Z be the zenith, M' and S' the apparent, and M and S the true places of the Moon and Sun or star, and z' and z the apparent and true distance respectively, and let the sides of the small triangles about M and S be named— MM' , δs , $M'L$ δz and SS' and SN δm and δz , respectively. It can easily be shown that when these triangles are very small *

$$\delta z = \delta s \left(\frac{\cos m \cdot \sin s - \sin m \cdot \cos s \cdot \cos Z}{\sin z} \right)$$

and the same, *mutatis mutandis*, applies to δz . The triangle connected with S will almost always be small enough, but that at M , when great accuracy is required, will generally need a small correction, but one that is very easily applied.

Taking an example from *Raper's Navigation* (p. 289 of 9th edit.)—

Apparent alt. of \odot $47^\circ 31'$, of \odot $36^\circ 52'$, app. dist. $48^\circ 20' 29''$. Sun's correction $47''$, that of \odot $45' 35''$.

First calculate the angle Z —in this step it is best to use logarithms to five figures—and whilst taking out the logarithms necessary for this step, take out also—to four places—those of the sin and cos of the side s diminished by half the parallax in altitude, and of m increased by $\frac{1}{2} 47''$.

$m' 42^\circ 29' 0''$	9.82954	Also 9.8296 and 9.8677 log cos m
$s' 53^\circ 8' 0''$	9.90311	„ 9.9009 „ 9.7819 „ s
$z' 48^\circ 20' 29''$	9.73265	
2) 143 57 29		
71 58 44	9.97815	
−48 20 29		
23 38 15	9.60309	
	9.58124	$Z = 65^\circ 42' 45''$. Its log cos 9.6142
	−9.73265	
	9.84859	

* $\cos z = \cos m \cdot \cos s + \sin m \cdot \sin s \cdot \cos Z$.

In this inquiry Z is always constant, and whilst considering the effects upon s and m separately, the opposed side m or s will be constant.

$$\therefore -\sin z \frac{dz}{ds} = -\cos m \cdot \sin s + \sin m \cdot \cos s \cdot \cos Z,$$

$$\text{and } \therefore dz = ds \left(\frac{\cos m \cdot \sin s - \sin m \cdot \cos s \cdot \cos Z}{\sin z} \right).$$

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a lunar distance.

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Then using the formula above given

$$L \cos m \ 9.8677 \quad L \sin m \ 9.8296$$

$$L \sin s \ 9.9009 \quad L \cos s \ 9.7819$$

$$+ 9.7686 \quad 9.6115$$

$$L \cos Z \ 9.6142$$

$$\text{No. } .5869 + \quad 9.2257 \quad \text{No. } .1682 \text{ negative}$$

Then

$$.5869$$

$$- .1682$$

$$.4187$$

$$\text{Its log } 9.6219$$

$$- L \sin z \ 9.8734$$

$$9.7485$$

$$+ \log \sin \delta s \ 8.1225$$

$$7.8710 \quad \text{Log sin } 25' \ 32'' .6. \text{ First approx. of } \delta z.$$

For dz_{II} use the same elements, but transposed :

$$\text{Log cos } s . \sin m \ 9.6115 \quad \text{Log sin } s . \cos m \ 9.7686$$

$$L \cos Z \ 9.6142$$

$$\text{No. } .4088 \quad 9.3828 \text{ No. } .2414 \text{ negative}$$

$$- .2414$$

$$.1674$$

$$\text{Its log } 9.2238$$

$$- L \sin z \ 9.8734$$

$$9.3504$$

$$+ \text{Log sin } 47'' \ 6.3577$$

$$5.7081 \quad \text{Log sin } 0' \ 10'' .5 = \delta z''$$

Hence the first correction of the distance is

$$25' \ 32'' .6 - 10'' .5 = 25' \ 22'' .1,$$

and the distance becomes $47^\circ 55' 7''$ as a first approximation. Now reduce the original distance by half the calculated correction, and use the sin of this value in the previous computation of δz ; or, what amounts to the same thing, apply to the final term the difference due to this reduced value of $\log \sin z$, which in this case (9.8719 instead of 9.8734) amounts to $+ .0015$, and the final term to 7.8725 , making $dz_1 = 25' 38''$.

The value of δz_{II} will not be altered appreciably, so the final correction is $25' 27'' .5$, and the distance $47^\circ 55' 1'' .5$.

A complete solution of this example, using logarithms to seven places, gives the distance $47^\circ 55' 0'' .88$.

It may be seen by the formula that when the angle Z is less than 90° if the second and negative term is greater than the first, the distance will be increased by the Moon's parallax in altitude, but in extreme cases the solar (or stellar) refraction may modify the general rule.

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Notes on Meteors observed at Penarth, Glamorgan, on 1896, Nov. 14. By George Carslake Thompson, LL.M., and H. W. Lloyd Tanner, M.A., F.R.A.S.

Our attention was mainly directed to the region of *Leo Major*. A building behind us cut off the western sky, some trees cut off the south, and we faced east or north-east. We both watched for about four hours after midnight with an interval specified in the following table. After 4 A.M. the observations were continued till 5.20 A.M. by Mr. Carslake Thompson alone. Each observation was recorded and rough notes were written at the time by G. C. T.

The entries in column A1 refer to meteors from the Sickie in *Leo*; A2, from the region above the Sickie; A3 from the region of β *Leonis* or the region between β and the Sickie. The entries in column B are of meteors from other directions. The directions of the meteors noted in column C were not determined.

Time.	A			B	C	Notes.
	1	2	3			
Soon after midnight	I	...	
12 35	I	
12 45	I	
12 52	I	
12 57	I	Short course with fine train; appeared 3 or 4 degrees eastward of Sickie; direction of course, perpendicular to and bisecting the line joining γ and ζ <i>Leonis</i> .
1 11	...	I	
1 30	I	Very faint and very short course; appeared very near ζ <i>Leonis</i> ; course inclined upwards at perhaps 30° to line joining γ and ζ .
1 34	I	
1 37	I	
1 47	I	
1 54	I	Fine train from direction ζ <i>Leonis</i> Maj. towards η or ζ <i>Ursæ</i> Maj.
1 54½	I	I	...	In same line; might have been same one coming into the air again.
1 58	
2 1	I	A very fine one; passed very close to ψ and γ <i>Ursæ</i> Maj. (perhaps half a degree above them) in a line parallel to the line joining these stars. Train persisted 2 or 3 seconds.